

SEE EXAMPLE 1 Given $f(x) = 8x + 13$ and $g(x) = x^2 - 5x$, find each function.
 2. $(f + g)(x)$ 3. $(f - g)(x)$ 4. $(g - f)(x)$

SEE EXAMPLE 2 Given $f(x) = 2x^2 + 2x$ and $g(x) = x + 1$, find each function.
 5. $(fg)(x)$ 6. $\left(\frac{f}{g}\right)(x)$ 7. $\left(\frac{g}{f}\right)(x)$

SEE EXAMPLE 3 Given $f(x) = 3x^2$ and $g(x) = 7 - x$, find each value.
 8. $f(g(5))$ 9. $g(f(5))$ 10. $f(g(-2))$

SEE EXAMPLE 4 Given $f(x) = x^2$, $g(x) = 2x - 3$, and $h(x) = \sqrt{x+1}$, write each composite function. State the domain of each.
 11. $f(g(x))$ 12. $g(f(x))$ 13. $f(h(x))$

PRACTICE AND PROBLEM SOLVING

Given $f(x) = 2x^2 - 8$, $g(x) = x^2 + 5x + 6$, and $h(x) = 2x + 4$, find each function.

- 15. $(f + g)(x)$
- 16. $(f - g)(x)$
- 17. $(f + h)(x)$
- 18. $(g - h)(x)$
- 19. $(fg)(x)$
- 20. $\left(\frac{f}{g}\right)(x)$
- 21. $\left(\frac{h}{f}\right)(x)$
- 22. $(gh)(x)$
- 23. $\left(\frac{g}{h}\right)(x)$

Given $f(x) = 2\sqrt{x+3}$ and $g(x) = -3x + 1$, find each value.

- 24. $f(g(1))$
- 25. $g(f(1))$
- 26. $f(g(4))$
- 27. $g(f(6))$
- 28. $f\left(g\left(\frac{4}{3}\right)\right)$
- 29. $g(f(97))$

Given $f(x) = 4x + 3$, $g(x) = \frac{x}{x+3}$, and $h(x) = -x^2 - 2$, write each composite function. State the domain of each.

- 30. $f(g(x))$
- 31. $g(f(x))$
- 32. $f(h(x))$

Use the tables to find each value.

- 39. $(g \circ f)(5)$
- 40. $(f \circ g)(3)$
- 41. $g(f(4))$
- 42. $f(g(2))$

x	2	3	4	5
f(x)	0	1	2	3

x	1	2	3	4
g(x)	1	2	4	8

43. **Critical Thinking** Can you use the tables to find $f(g(4))$? Explain your answer.

45. If $(f \circ g)(x) = (3x + 4)^2$, which of the following could be true?

- (A) $f(x) = 3x + 4$ and $g(x) = x^2$
- (B) $f(x) = x^2$ and $g(x) = 3x + 4$
- (C) $f(x) = (3x)^2$ and $g(x) = 4^2$
- (D) $f(x) = 3x + 4$ and $g(x) = \sqrt{x}$

46. If $f(x) = 2x + 1$ and $g(x) = 5x - 2$, then which of the following is $(fg)(5)$?

- (F) 253
- (G) 53
- (H) 47
- (J) 13

47. Given $f(x) = 4 - x^2$ and $g(x) = \frac{1}{2}x - 2$, which of the following is $(f \circ g)(x)$?

- (A) $(f \circ g)(x) = -\frac{1}{2}x^2$
- (B) $(f \circ g)(x) = -\frac{1}{4}x^2 + 2x$
- (C) $(f \circ g)(x) = -\frac{1}{2}x^3 + 2x^2 + 2x - 8$
- (D) $(f \circ g)(x) = -x^2 + \frac{1}{2}x + 2$

$$\begin{aligned}
 f(g(x)) &= f\left(\frac{1}{2}x - 2\right) \\
 &= 4 - \left(\frac{1}{2}x - 2\right)^2 \\
 &= 4 - \left(\frac{1}{2}x - 2\right)\left(\frac{1}{2}x - 2\right) \\
 &= 4 - \left(\frac{1}{4}x^2 - 2x + 4\right) \\
 &= -\frac{1}{4}x^2 + 2x
 \end{aligned}$$

$$\begin{aligned} 30. \quad f(g(x)) &= \\ f\left(\frac{x}{x+3}\right) &= \frac{4}{1}\left(\frac{x}{x+3}\right) + 3 \\ &= \frac{4x}{x+3} + 3^{(x+3)} \\ &= \frac{4x}{x+3} + \frac{3x+9}{x+3} \\ &= \frac{7x+9}{x+3} \end{aligned}$$

$$\frac{g(f(x))}{g(4x+3)} = \frac{\frac{4x+3}{4x+3+3}}{\frac{4x+3}{4x+6}}$$